

EVIDENCE GUIDED NOTES

Term	Definition
Proof	Logical argument that shows a statement is true
Justify	Layout your mathematical thought process step by step
Geometric proof	Given Geometry based statements that prove a mathematical concept is true
Types of proofs	Two-Column and Paragraph

Reasons Word Bank

Definitions	Properties
<ul style="list-style-type: none"> • Definition of Angle Bisector • Definition of Complementary Angles • Definition of Congruent Angles • Definition of Congruent Segments • Definition of Linear Pair • Definition of Midpoint • Definition of Right Angles • Definition of Segment Bisector • Definition of Supplementary Angles • Definition of Vertical Angles 	<ul style="list-style-type: none"> • Addition Property of Equality • Distributive Property • Division Property of Equality • Multiplication Property of Equality • Reflexive Property • Substitution Property of Equality • Subtraction Property of Equality • Symmetric Property • Transitive Property
Postulates	Theorems
<ul style="list-style-type: none"> • Angle Addition Postulate • Linear Pair Postulate • Segment Addition Postulate 	<ul style="list-style-type: none"> • Alternate Exterior Angles Theorem • Alternate Interior Angles Theorem • Angle Bisector Theorem • Consecutive Interior Angles Theorem • Corresponding Angles Theorem • Midpoint Theorem • Vertical Angles Theorem

Algebraic Proof

Given: $2x + 5 = 20 - 3x$

Prove: $x = 3$

Statement	Reason
1. $2x + 5 = 20 - 3x$	1. Given
2. $5x + 5 = 20$	2. Addition Property of Equality
3. $5x = 15$	3. Subtraction Property of Equality
4. $x = 3$	4. Division Property of Equality

All students should be able to solve an equation for x . Explain to students that there is more than one way to solve the given equation. A student could have solved the problem a different way, and still get the correct answer.

Sample Explanation of Algebraic Proof:

Was everyone able to solve this equation and get $x = 3$? Great, now let's talk about the reasons column. The purpose of the reasons column is to prove why the statement is true, in this case, we are proving why $x = 3$.

Where did we get the first statement? It was given to us. "Given" is our reason.

How did we get to statement 2? We added $3x$ to both sides. We were able to do that because of the Addition Property of Equality.

How did we get statement 3? We subtracted 5 from both sides. We were able to do that because of the Subtraction Property of Equality.

How do we get statement 4? We divided 5 on both sides. We were able to do that because of the Division Property of Equality.

Creating a Proof

Given: $AC = AB + AB$



Prove: $AB = BC$

Statement	Reason
1. $AC = AB + AB$	1. Given
2. $AB + BC = AC$	2. Segment Addition Postulate
3. $AB + BC = AB + AB$	3. Transitive Property
4. $BC = AB$	4. Subtraction Property

Paragraph Proof

Given, $AC = AB + AB$ we know that the equation $AB + BC = AC$ can be written because of the Segment Addition Postulate. $AB + BC = AB + AB$ because of the Transitive Property. Both sides of the Equation contain AB , therefore through the Subtraction Property, $BC = AB$.

Sample explanation of creating the proof:

We should always start a proof by filling out the given information. You will be surprised how much of your proof is already done with the given information included. The first statement of every proof is the “given” statement from the question. The last statement of every proof is the “prove” statement from the question. The first reason of every proof is “Given”.

I know that this question is asking me to prove that each ‘half’ of this segment is equal, so I have to do 2 things:

1. Prove that point B is the midpoint of this segment for that to be true.
2. Get to a place where BC is a statement in the proof before line 4.

We have learned about the segment addition postulate, so let’s use that for the given picture.

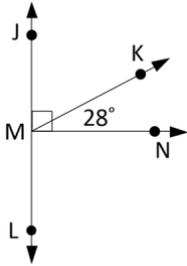
I notice that the addition problem in line 1 and line 2 both equal the same segment. If they equal the same thing, then they will equal each other because of the Transitive Property.

In line 3 do you see how segment AB is on both sides of the equation? What happens to this equation if I choose to subtract AB from both sides to eliminate it? (You get the last statement of the proof!)

Completing a Proof

Given: $\angle KMN = 28^\circ$

Prove: $\angle JMN = 90^\circ$



Statement	Reason
1. $\angle KMN = 28^\circ$	1. Given
2. $\angle JMK$ and $\angle KMN$ are Complementary Angles	2. Given
3. $\angle JMK + \angle KMN = \angle JMN$	3. Angle Addition Postulate
4. $\angle JMK + \angle KMN = 90^\circ$	4. Definition of Complementary Angles
5. $\angle JMN = 90^\circ$	5. Transitive Property

Sample explanation for completing the proof:

In math, we usually complete the proof more than creating the proof because it provides more guidance to you guys and helps train you to take the direct route to answer a problem and not waste your time providing too much information.

To start our proof there are 3 lines we can add that requires no thought on your part. (Statement 1 & 4, Reason 1) Copy the Given and Prove into your statements and the first reason will always be Given.

At this point, you only have to come up with 2 reasons and you're done! Let's look at the statements and give them a reason just as we did with Elle's argument.

Statement 2: angle + angle = a larger angle. You should notice that this is like line 2 of the last proof except it is naming angles instead of segments. This is the angle addition postulate.

Looking at statement 2 and 3 you will notice that $JMK + KMN$ added together equal 90 degrees but added together they also equal JMN . Since the left side of both of those equations are the same, I can use the Transitive Property to take out the repeated parts and set the right side of each equation equal to each other.